Interpreting ISR Data

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(With thanks and appreciation to Mike Lockwood)

ISR data: What to be aware of

- With ISR data, what you get out depends significantly on what you put in!
 ...so be aware of what that is.....
- When you choose your experiment you start constraining your science
 - frequencies,
 - coding,
 - pointing/ scanning,
 - resolution

ISR data: What to be aware of

- Analysing the data implies more constraints
 - Integration times
 - Range/altitude resolution
 - Non-thermal spectra
 - Satellites, space debris, clutter
 - Fit ambiguities and covariance
 - Systematic errors due to (possibly) incorrect assumptions
 - Modelled compositions
 - Collision frequencies
 - Iteration limits
 - Convergence criteria
 - Random errors

The danger is not to realise that these effects exist!

What this talk is and isn't....

- This talk is partly about some of the problems that can happen with your experiment, data integration and fitting.
- This talk is mainly to get you thinking about the physical meaning of the results, especially for high latitude radars.
- Even if you've designed a perfect experiment and done a perfect analysis, the interpretation is not necessarily simple....



Usual Summary Plot Format

These data show what? (is anyone colourblind?)

Data plotted as a function of UT of observations and altitude of range "gate"





Usual Summary Plot Format

These data show what?

Data plotted as a function of UT of observations and altitude of range "gate"



Fixed field-aligned data



Electron number density, N_e (m⁻³)

Electron temperature, T_e (K)

lon temperature, T_i (K)

Line–of–sight velocity, V_{los} (ms⁻¹)

Random Errors in EISCAT (CP1) Data





Coherent echoes

(will appear as bad data in summary plots)

Anomalous echoes



Other examples: satellites, meteor echoes, heater effects, other non-thermals..

Fixed field-aligned data



Electron number density, N_e (m⁻³)

Electron temperature, T_e (K)

lon temperature, T_i (K)

Line–of–sight velocity, V_{los} (ms⁻¹)

What about these data?



Electron number density, N_e (m⁻³)

Electron temperature, T_e (K)

lon temperature, T_i (K)

Line-of-sight velocity, V_{los} (ms⁻¹)

Altitude and Pointing Direction vertical, e.g. CP7, (r / h) = 1, $\Delta \lambda_G = 0$, $\Delta \lambda_M > 0$ magnetic inclination < 90° elevation =90° range r is the same as height, h range of geographic latitude $\Delta \lambda_G = 0$ range of geomagnetic latitude $\Delta \lambda_M > 0$ h=0



Altitude and Pointing Direction

Field-aligned, e.g. CP1, (r / h) > 1, $\Delta \lambda_M = 0$, $\Delta \lambda_G > 0$





Fixed field-aligned data



Electron number density, N_e (m⁻³)

Electron temperature, T_e (K)

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Line–of–sight velocity, V_{los} (ms⁻¹)

What about these data?



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Changing Pointing Direction









Definition of Temperature

(distribution functions)



Number of particles in unit volume = N

In cube shown, the number density, N = 1 m⁻³

Distribution function (or phase space density) is the number of particles in unit volume with a given vector velocity

Here $f(\underline{V})=1$ for $\underline{V} = \underline{V}_1$ but $f(\underline{V})=0$ for all other \underline{V} (i.e., $f(\underline{V})$ is a delta function in this simple case)

In general, in unit volume, the number of particles with X-velocity between V_x and V_x+dV_x and with Y-velocity between V_y and V_y+dV_y and with Z-velocity between V_z and V_z+dV_z is f(<u>V</u>)dV_xdV_ydV_z = f(<u>V</u>)d³<u>V</u>

> Number density, N = $\int_{-\infty}^{+\infty} f(\underline{V}) d^3 \underline{V}$ (m⁻³) Units of $f(\underline{V})$ are m⁻³/ (ms⁻¹)³ = m⁻⁶s³



Line-of-sight temperature

(derivation courtesy Jean-Pierre St-Maurice)

For a direction that makes an aspect angle ϕ with the magnetic field, along which the velocity is V_{ϕ}

Definition of 1D temperature T_{ϕ} : $\langle V_{\phi}^2 \rangle = k_B T_{\phi}/m_i = (1/N) \int_{-\infty}^{+\infty} V_{\phi}^2 f(\underline{V}) d^3 \underline{V}$ Where $f(\underline{V})$ is the distribution function and $d^3 \underline{V} = dV_X dV_Y dV_Z$ If gyrotropic, $f(\underline{V}) = f(V_X, V_Y, V_Z) = f(V_{||}, V_{\perp})$ $V_{\phi} = V_{||} \cos \phi + V_{\perp} \sin \phi$ $V_{\phi}^2 = V_{||}^2 \cos^2 \phi + V_{\perp}^2 \sin^2 \phi + 2V_{||} V_{\perp} \cos \phi \sin \phi$ Substitute

$$\begin{aligned} \mathsf{k}_{\mathsf{B}} \ \mathsf{T}_{\phi}/\mathsf{m}_{\mathsf{i}} &= \ \int_{-\infty}^{+\infty} \ \mathsf{V}_{||}^{2} \cos^{2}\phi \ \mathsf{f}(\mathsf{V}_{||},\mathsf{V}_{\perp}) \ \mathsf{d}^{3}\underline{\mathbf{V}} + \int_{-\infty}^{+\infty} \ \mathsf{V}_{\perp}^{2} \sin^{2}\phi \ \mathsf{f}(\mathsf{V}_{||},\mathsf{V}_{\perp}) \ \mathsf{d}^{3}\underline{\mathbf{V}} \\ &+ 2 \int_{-\infty}^{+\infty} \ \mathsf{V}_{||} \ \mathsf{V}_{\perp} \sin \phi \ \cos \phi \ \mathsf{f}(\mathsf{V}_{||},\mathsf{V}_{\perp}) \ \mathsf{d}^{3}\underline{\mathbf{V}} \end{aligned}$$



Line-of-sight temperature

$$k_{\rm B} T_{\phi}/m_{\rm i} = \int_{-\infty}^{+\infty} V_{||}^{2} \cos^{2}\phi f(V_{||},V_{\perp}) d^{3}\underline{V} + \int_{-\infty}^{+\infty} V_{\perp}^{2} \sin^{2}\phi f(V_{||},V_{\perp}) d^{3}\underline{V}$$
$$+ 2 \int_{-\infty}^{+\infty} V_{||} V_{\perp} \sin \phi \, \cos \phi f(V_{||},V_{\perp}) d^{3}\underline{V}$$

If the distribution function is also symmetric along <u>B</u> $f(V_{||},V_{\perp}) = f(-V_{||},V_{\perp})$, so $\int_{-\infty}^{+\infty} V_{||} f(V_{||},V_{\perp}) d^3\underline{V} = 0$ and the 3rd term in RHS of above equation is zero

Subs for
$$\phi = 0$$
 $k_B T_{\phi}/m_i = k_B T_{||}/m_i = (1/N) \int_{-\infty}^{+\infty} V_{||}^2 f(V_{||}, V_{\perp}) d^3 \underline{V}$
Subs for $\phi = \pi/2$ $k_B T_{\phi}/m_i = k_B T_{\perp}/m_i = (1/N) \int_{-\infty}^{+\infty} V_{\perp}^2 f(V_{||}, V_{\perp}) d^3 \underline{V}$

Yields
$$T_{\phi} = T_{||} \cos^2 \phi + T_{\perp} \sin^2 \phi$$
$$(c.f. \quad V_{\phi} = V_{||} \cos \phi + V_{\perp} \sin \phi)$$



3-D temperature

Three Dimensional temperature: $\exists k_B T/m_i = \langle V^2 \rangle = (1/N) \int_{-\infty}^{+\infty} V^2 f(\underline{V}) d^3 \underline{V}$ Where $V^2 = V_X^2 + V_Y^2 + V_Z^2$ $\exists k_B NT/m_i = \int_{-\infty}^{+\infty} V_X^2 f(\underline{V}) d^3 \underline{V} + \int_{-\infty}^{+\infty} V_Y^2 f(\underline{V}) d^3 \underline{V} + \int_{-\infty}^{+\infty} V_Z^2 f(\underline{V}) d^3 \underline{V}$

$$\begin{aligned} 3k_{B}T/m_{i} &= (k_{B}/m_{i}) \{T_{X} + T_{Y} + T_{Z}\} \\ \text{Gyrotropic, so } T_{X} &= T_{Y} = T_{\perp} \text{ and } T_{Z} = T_{||} \\ T &= (T_{||} + 2T_{\perp}) / 3 \end{aligned}$$
The magic angle $\phi = \phi_{M}$ where $T = T_{\phi}$

$$(T_{||} + 2T_{\perp}) = 3 \{T_{||} \cos^{2}\phi_{M} + T_{\perp} \sin^{2}\phi_{M} \}$$

$$\sin(\phi_{M}) = (2/3)^{1/2}$$

$$\phi_{M} = 54.7^{\circ}$$



What about these data?



Electron number density, N_e (m⁻³)

Electron temperature, T_e (K)

lon temperature, T_i (K)

Line-of-sight velocity, V_{los} (ms⁻¹)




























Latitude or altitude?

- How can we tell whether we are observing a latitude-dependent process or an altitudedependent process?
- We can use our knowledge of atmospheric physics to determine which kind of variation is the more likely.
- Sometimes this is easy, because certain parameters do not change with height.



Height Profiles



 T_i , V_{\perp} and $V_{||}N_e$ are approximately independent of h above about 200 km. Thus we can identify latitudinal structures and motions in these variables



T_i Profiles

Why is T_i independent of h?

Ion energy balance equation

Time derivative $d(N_i k_B T_i)/dt$ negligible on timescales > $(1/v_{in})$ ~ 1sec

Viscosity negligible on spatial scales > ~ 1km

Strictly, the divergence of heat flux $\nabla .q_i$ and the advection term $\underline{V}.\nabla$ $(N_ik_BT_i)$ are not always negligible but this is a good approximation at h < ~500km. Gives

$$Q_i - L_i = 0$$

Where the heat gained by the ion gas is the effect of collisions with the n neutral species which transfer some of their energy (of both thermal motions and bulk flow motions)

 $Q_{i} = \sum_{n} N_{i} m_{i} v_{in} \{ 3k_{B}(T_{n} - T_{i}) \psi_{in} + m_{j} (V_{i} - V_{n})^{2} \phi_{in} \} / (m_{i} + m_{n})$

And the velocity dependent correction factors ϕ_{in} and ψ_{in} are close to unity.



T_i Profiles

Why is T_i independent of h?

Loss term L_i is heating of electron gas by collisions of ions with electrons (in fact it is a loss L_i > 0 if T_e < T_i, but another gain L_i > 0 if T_e < T_i). From same equation for electrons, for which $m_i/(m_e+m_i) \approx 1$

$$L_{i} = -N_{e}v_{ie} \{ 3k_{B}(T_{e}-T_{i}) + (V_{i}-V_{e})^{2} \}$$

$$\begin{split} & Q_i - L_i = 0 \text{ gives} \\ & T_i = T_n + (m_n/3k_B) \; (\varphi_{in}/\psi_{in}) \; (V_i - V_n)^2 \; + \; (v_{ie}/v_{in}) \; \{(m_i + m_n)/m_i\} \; (T_e - T_i) \; / \psi_{in} \\ & \text{For } \varphi_{in} = \; \psi_{in} = 1, \end{split}$$

O⁺ ions and O atoms (F-region ionosphere), $\{(m_i+m_n)/m_i\} = 2$

 $(m_n/3k_B) = 6.46 \times 10^{-4} \text{ kg K J}^{-1} (\text{in SI units})$

Because $T_e \sim T_i$, the second term on the RHS is usually negligible $T_i = T_n + 6.46 \times 10^{-4} (V_i - V_n)^2$

 T_n , $V_i\!,$ and V_n are all roughly independent of h-so is T_i



Perpendicular ion velocity

Why is V₁ independent of height above about 210 km?



* w.r.t. neutral gas



Flux Profiles

Why is N_eV₁₁ independent of h?

Continuity equation on a flux tube



 $d(N_iAV_{11})/dh = q - L$

Above h of about 200 km production q and loss L are negligible

(note we consider total ion flux so charge exchange is not a factor)

(1/F) dF/dh = (1/A) dA/dh

In the ionosphere A(h) is approximately constant (and is known from magnetic field model) so F is approximately constant)





CP-4-A (UHF), azimuth 2 (points Magnetic north)



N_e and T_e - latitude structure and height structure mixed for this low elevation beam

Look at one height at a time to see time variations

 T_i and $V_{los} \approx V_{\perp N}$ approx. indep. of h and so this is a latitudinal structure and it migrates poleward



A Polar Cap Contraction CP-4-A (UHF), azimuth 1 (points 12° east of magnetic north)



N_e, T_e and Ti show the same features as aximuth1 – gives us a orientation w.r.t. the L-shells and a minimum extent

V_{los} is quite different to that for azimuth 1 – shows either longitudinal structure or, more likely, along L-shell convection



CP-4-A, both azimuths



structure and differences show show best if both azimuths are interleaved on the same plot

Vertical stripes in V_{los} highlight the differences between the two beams



Beamswinging E vectors superposed on T_i plot

Note band of high T_i is only on trailing side of convection reversal boundary (OCB)





Where are we?

F-o-v is north of Tromsø (latitudes $\lambda = 70.5 - 74.5^{\circ}$)

For this f-o-v MLT ≈ UT + 1.75 hrs

(use, e.g. http://lewes.gsfc.nasa.gov/space/cgm/cgm.html)

Poleward-moving event is at about 4:00UT, ≈ 5:45 MLT, i.e. near dawn





Where are we?

In fact there is an asymmetry in observed V_{los} , flow – as shown below It reveals that there is flow across the convection reversal boundary





A Polar Cap Contraction What's going on? Substorm recovery phase

growth phase



expansion and recovery phases

In substorm recovery phase, reconnection voltage in cross-tail current sheet (that destroys open flux) exceeds that at the dayside magnetopause (which generates open flux) and so the open polar cap contracts.





Ion-neutral frictional heating event

Caused by polar cap contraction

 $T_i = T_n + (m_n/3k_B) |\underline{V}_i - \underline{V}_n|^2$

 $N_n >> N_i$; means that responses in \underline{V}_n to changes of \underline{V}_i are small and slow





Ion-neutral frictional heating event

Caused by polar cap contraction



Boundary moves so ion flows reverse in band between old and new locations

Neutrals do not respond for a while. In the band $\underline{V}_n = -\underline{V}_i/3$ $(\underline{V}_i - \underline{V}_n)^2 = (4V_i/3)^2 = (16/9)V_i^2$ So this term is 4 times larger For the typical $V_i = 1$ kms⁻¹ and $T_n \approx 800$ K eqn. gives $T_i \approx 1950$ K



Beamswinging E vectors superposed on T_i plot

Note band of high T_i is only on trailing side of convection reversal boundary (OCB)





Ion-neutral frictional heating event

Caused by polar cap contraction

 $T_i = T_n + (m_n/3k_B) |\underline{V}_i - \underline{V}_n|^2$

high Ti in this band slowly subsides as neutral begin to respond





Substorm Cycles

(in CP-4-B data)



See expansions and contractions. This time MLT ≈ UT + 2.75hr

So 06-12 UT is 8:45-12:45 MLT



Substorm cycles

Use solar wind and magnetic indices to understand the radar data





Substorm cycles Note: changing the contour levels often helps you see an event





Inferred Open-Closed Boundary

(agrees well with DMSP passes over the cusp)

ALWAYS check as much supporting data as exists from other sources as you possibly can!





Polar Cap Patches

(in same CP-4-B data)





^{*} Not TOO bad an assumption in the lower topside



Observed density N_e corrected to reference height h_o by assuming diffusive equilibrium to give N_{eo} = $N_e(h) / f(h)$

Polar Cap Patches





Polar Cap Patches in N_e

If N_e falls in patch as it moves poleward is it

A. because N_e is lower at greater h?

Or

B. because patch has moved in MLT?

Low-elevation Radar Beam



Polar Cap Patches in N_{eo}

If N_{eo} falls in patch as it moves poleward we KNOW it is

B. because patch has moved in MLT

(because N_{eo} does not depend on h) Low-elevation Radar Beam



Phase Motion $V_x = \Delta x / \Delta t$

(use lag ∆t from cross-correlation)





Phase Motion $V_x = \Delta x / \Delta t$

(use lag ∆t from cross-correlation)

A word of warning: you need to worry about event orientation (relative to two points A and B used) Event at time (t + At) phase velocity normal to event is $V_{pn} = \Delta x(\cos \alpha) / \Delta t$ true phase velocity $V_p = \Delta x (\cos \alpha / \cos \beta) / \Delta t$ Vpn Event at time t Δx ß



CP1 – Field-aligned

(a winter run lasting 3 days)


























A precipitation event

(the passage of an auroral arc)

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The bottom of arcs are near h = 110 km.

For field-aligned beam r \approx 120 km

EISCAT beamwidth \approx 0.5° (FWHM), d\theta = 0.5\pi/180 rads

Beam diameter = r d\theta \approx 1 km

Arcs are sometimes less than 100m

Arcs can move at 5 km s<sup>-1</sup> – would cross the beam in just 0.2 s
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Therefore want high time resolution for arc studies

Tromsø, 30 January 1995



Solar-Terrestrial Physics



A precipitation event

(dispersion structure)

In the rest frame of the arc

(in the radar rest frame, the arc moves over radar in same direction as convection, but is moving more slowly then convection)





CP1 – Field-aligned

(a typical winter day)

Dayside maxima in N_e (and T_e)





CP1 – Field-aligned

(a typical summer day)



Note T_e and, by electron ion conduction T_i are also much greater than in winter case

EISCAT - Emc - Longyearbyen - 2009-05-04 Problem of Ion Composition

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Large Scans (e.g. CP3)

(summary plot dominated by the beam scan pattern)



Summary plot hard to interpret because of scan pattern.

But can make out basic Ne and T_e variation as seen for CP1

Stripes with scan period (30 min) reveal latitudinal structure

500





Scan up - spin - and scan down



Large Scans (e.g. CP3)

(summary plot dominated by the beam scan pattern)







Working out where the radars were

e.g. Using Iceland CUTLASS SuperDARN HF radar

(can use IMAGE magnetometer chain & Imagers also)

Transient westward flow burst

> Here ESR is just poleward of CRB (Convection Reversal Boundary)





Putting ESR and Cluster data into context

Using SuperDARN radar convection maps and imagers





Putting the field-aligned data in context

using 2 ESR beams

- effect of northward turning
- motions over radar matched to those over Cluster
- poleward-moving events shown to be caused by lowenergy electron flux changes
- transient LLBL and cusp entries shown to be FTEs





Field-aligned flows

(put into context of a TCV using IMAGE magnetometers)

SW pressure pulse arrival time









Identifying the cusp (DMSP satellite pass) and the open-closed boundary (OCB)







Model simulations of cusp electron precipitation effects on a newly-opened field line convecting through cusp. Precipitation is present for elapsed times since reconnection of about 150-750 s.

Davis and Lockwood, Annales Geophys., 14, 1246-1256, 1996.



Identifying the cusp (Photometer)

McCrea et al., Annales Geophys., 18, 1009-1026, 2000.

In cusp red line dominant, but there is always some green





Identifying the cusp (ESR and CP4) McCrea et al., Annales Geophys., 18, 1009-1026, 2000.

NE (m^a)

TE (K)

2/00×101 1,81×101

1.62=10

1.43×10

1.24×10

1.05×10

8,60×10

8.70=1010

4.80x1010

2.99 - 10 10 1.00×10

3500

2800

2450

2100

1750

1400

1050

700

300

3503

2000 2450

2100

1750

1400

1050

700

350

100

80

60

40

20

-20

-40

-60

80

-100

0

TI (k)







Lockwood et al, Ann. Geophys., 18, 1027–1042, 2000





Identifying the cusp (ESR 32m – looking north)





Identifying the cusp (ESR 42m – field aligned)





Plasma density profile



Sub-

auroral

Polar Cap

Electron temperature profile



Cusp – outside 630nm transient Cusp – inside 630nm transient



High F-region electron density N_e (but can be confused with EUV-enhanced polar cap patches convecting poleward)

High Electron Temperature (patches of subaurorally EUV-produced plasma would not show enhanced T_e)

Electron density highly variable in cusp – gives poleward-moving 630nm transient aurorae

Conclusions(I)

- When interpreting your data, remember....
 - The ISR technique contains ambiguities
 - Range/Doppler ambiguity is inherent
 - Noise is always present, giving uncertainty
 - Be careful of over-interpreting your data
- At high latitudes, remember....
 - Ionosphere can be highly structured in latitude and longitude
 - Ionosphere can be dynamic, e.g. responding to changing solar wind conditions
 - Looking anywhere but along B, you will convolve altitudedependence with latitude/longitude dependence
 - Some tricks are available to test which might be which
 - Even looking field-aligned, the time series data can conditioned by latitude/longitude variation (features moving across the radar)

Conclusions(II)

- Good experiment design is critical
 - A well-designed experiment really aids understanding
 - Think about characteristic times, scale sizes of events and the measurements needed to characterise them.
 - A badly-designed experiment can produce seriously misleading conclusions (or none)

Context is all important....

- Remember that what you see is limited by your experiment
- ISR is a very powerful technique, but not an oracle!
- Using multiple radars or other diagnostics is key to determining what might be going on
The Wisdom of JP....

- "Let the data speak!...."
- "...but don't torture it...."



"If your torture your data enough, it will confess to anything..."



The End

(does anyone have any questions?)





Special Programmes (SP)

(for which we might not know beam scan pattern)







Field-aligned flows

(seen using ESR)



Note upflows (red away from Earth) in bottom





Tromsø, 30 January 1995



Solar-Terrestrial Physics